

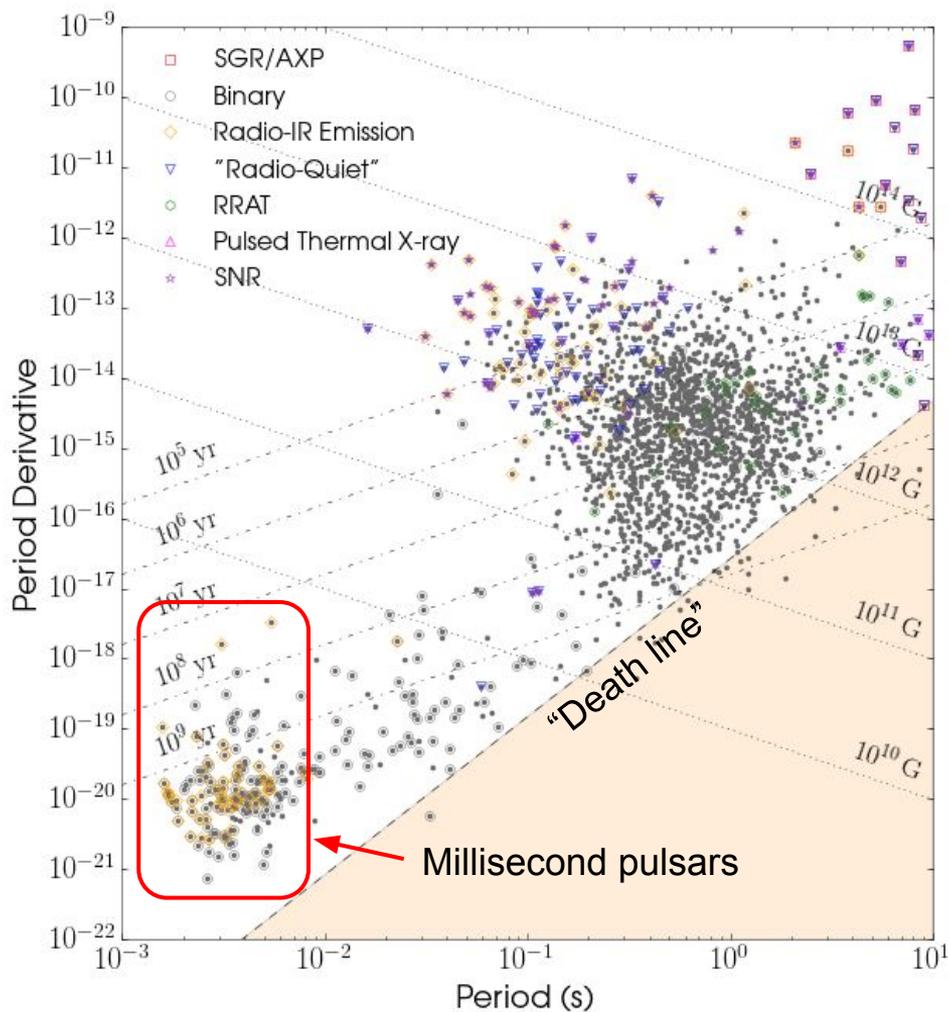
# Evidence for a minimum pulsar ellipticity?

(G. Woan, M. Pitkin, B. Haskell, D. I. Jones & P. Lasky,  
*ApJLett*, **863**, L40 (2018), [arXiv:1806.02822](#))

# The P-Pdot diagram

We can plot the period of known pulsars against their period derivative - Pdot (*observed Pdot and true Pdot are not necessarily the same!*)

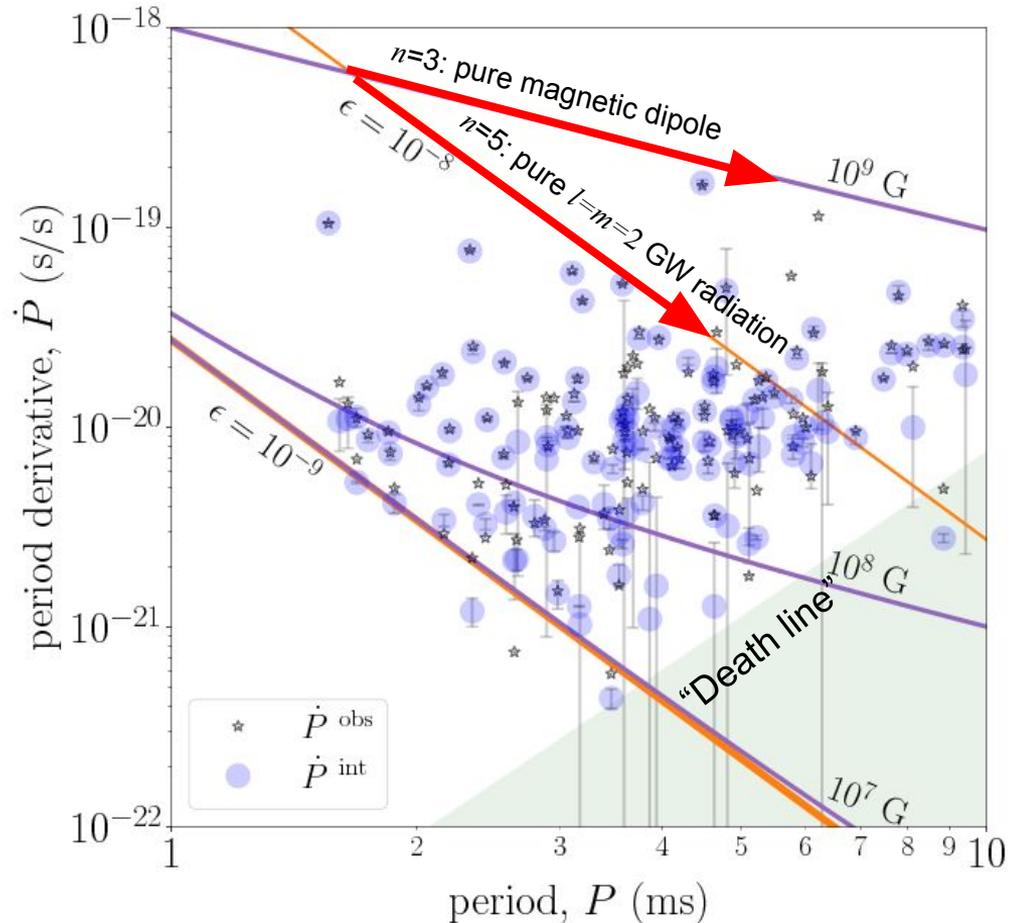
- lines for different external dipole magnetic field strengths (assuming pure magnetic dipole braking)
- lines for different *characteristic* ages



# P-Pdot diagram

Zoom in on MSPs (showing intrinsic Pdot and uncertainties)

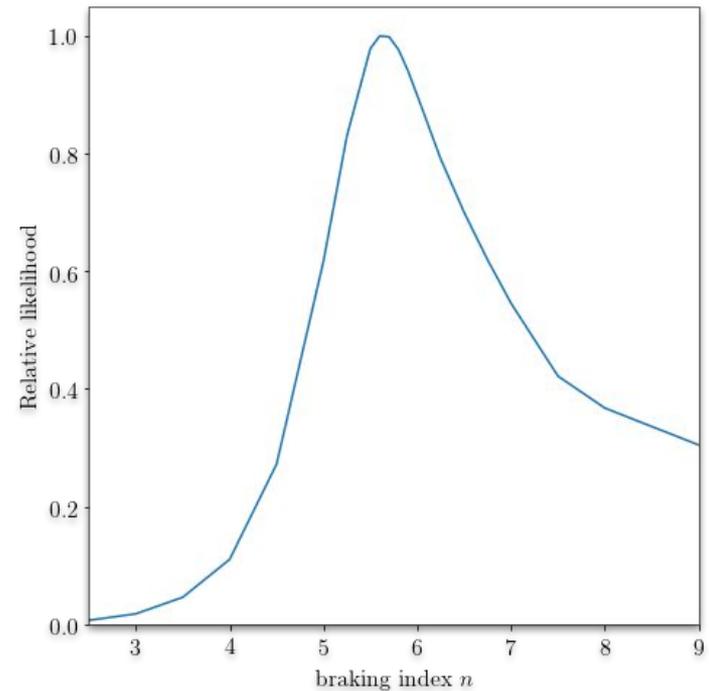
- Lines showing evolution contours for stars spinning-down via
  - pure magnetic dipole radiation
  - pure  $l=m=2$  GW emission
  - a combination of both
- Lack of pulsars below contour for GW emission assuming pulsars with ellipticities of  $10^{-9}$ !?



# Ellipticity cut-off

Is the ellipticity cut-off real?

- Observational selection effects?
  - No obvious selection effects that we know of
- Statistical sanity check
  - Prior that MSPs are log-uniformly distributed in  $\dot{P}$ , with a lower  $\dot{P}$  cut-off combining a “death line” (for the r.h.s. of the diagram) and a power law braking process cut-off with unknown braking index (slope) and scale; how do fits to the data including different braking index cut-offs compare to no cut-off?
  - Incorporate uncertainties on  $\dot{P}$  values and in pulsar moment of inertia



Cut-off with  $n=5$  (i.e. pure GW emission) favoured over no cut-off by  $\sim 6400$

Cut-off with  $n=5$  favoured over  $n=3$  (i.e. pure magnetic dipole emission) by  $\sim 35$

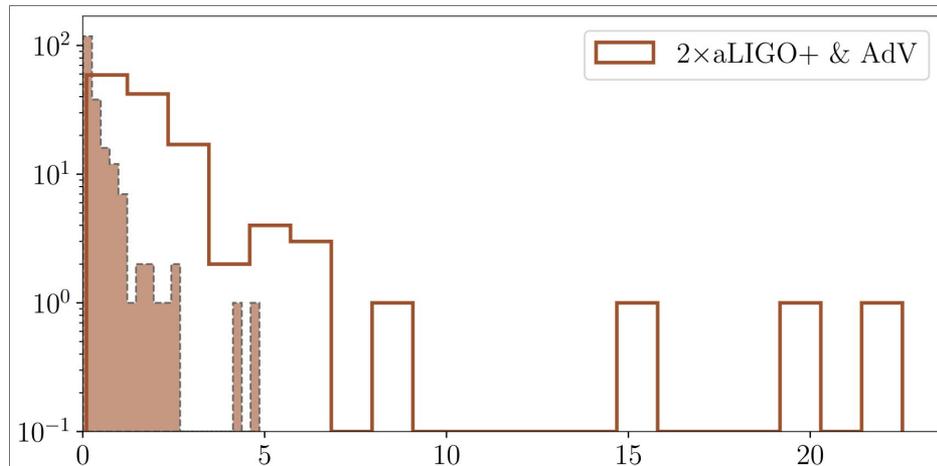
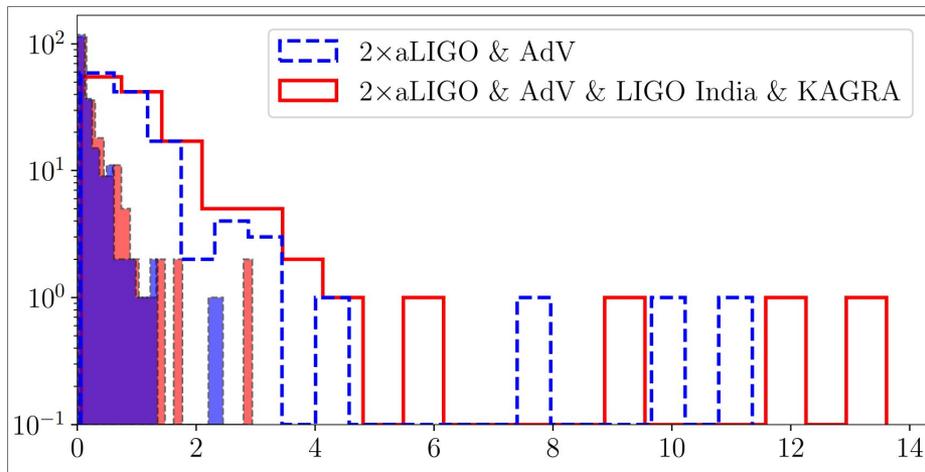
Best fit ellipticity for  $n=5$  is  $\sim 10^{-9}$  (for moment of inertia of  $10^{38}$  kg m<sup>2</sup>)

# Ellipticity cut-off

What could cause a minimum ellipticity in MSPs?

- MSPs are recycled; they underwent an accretion phase in a binary system to spin them up
  - Small external magnetic field for MSPs ( $\sim 10^8$  Gauss) compared to “young” pulsars ( $\gtrsim 10^{11}$  Gauss) suggests field may have been “buried” during accretion (e.g., [Vigelius & Melatos, \*MNRAS\*, 395, 2009](#))
    - old and cold MSPs may have cores that are type II superconductors, so ellipticity is linear in internal field strength (e.g., [Lander, \*MNRAS\*, 437, 2014](#)) with  $\epsilon \sim 10^{-8}(B_i/10^{12} \text{ Gauss})$  - so  $\epsilon \gtrsim 10^{-9}$
  - Asymmetric crustal fracturing during spin-up ([Fattoyev \*et al.\*, arXiv:1804.04952](#)), or spin-down (e.g., [Baym & Pines, \*AnPhys\*, 66, 1971](#)), could imprint a similar ellipticity in all MSPs

# Implications for GW detections

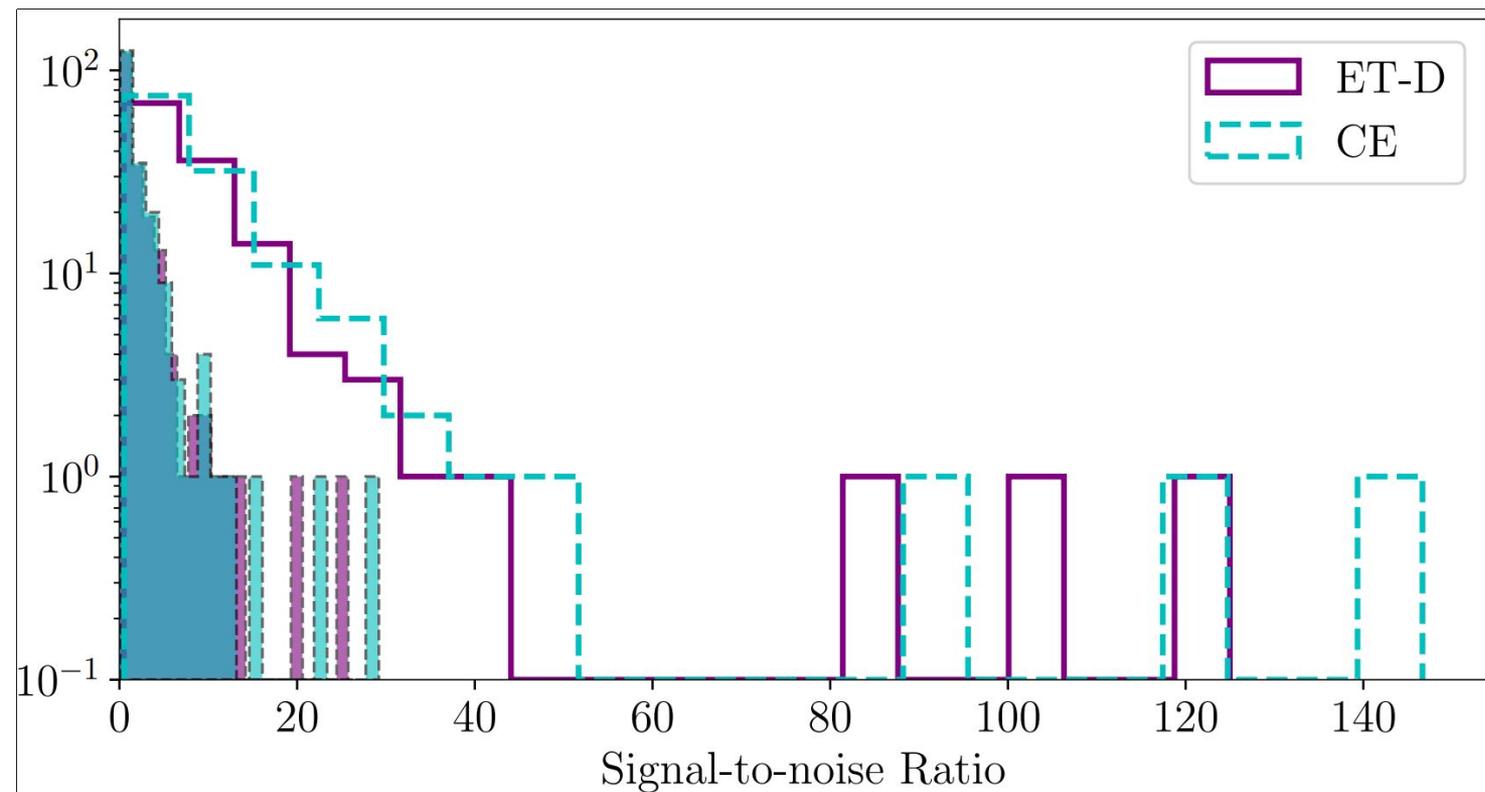


Expected SNR for one year coherent observations of pulsars with various detector networks:

- Filled histograms - all pulsars with ellipticities of  $10^{-9}$
- Unfilled histograms - all pulsars emitting at their spin-down limits

# Implications for GW detections

Assuming all have  
 $\epsilon=10^{-9}$



ET:

- SNR > 20: **2**
- SNR > 15: **2**
- SNR > 10: **5**
- SNR > 8: **9**
- SNR > 5: **15**

CE:

- SNR > 20: **2**
- SNR > 15: **3**
- SNR > 10: **6**
- SNR > 8: **9**
- SNR > 5: **18**