

GWD beyond SQL with the negative mass spin oscillator

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X, P – noncommuting variables

Standard Quantum Limit
for motion of a free mass

$$X(t) = X + \frac{Pt}{m}, \quad \Delta X \Delta P \geq \frac{\hbar}{2} \Rightarrow$$
$$[\Delta X(t)]^2 \geq (\Delta X)^2 + \frac{\hbar^2 t^2}{4m^2(\Delta X)^2} \geq \frac{\hbar t}{m} \quad (\text{SQL})$$

Motion in reference frame with *negative mass*

Slide 3

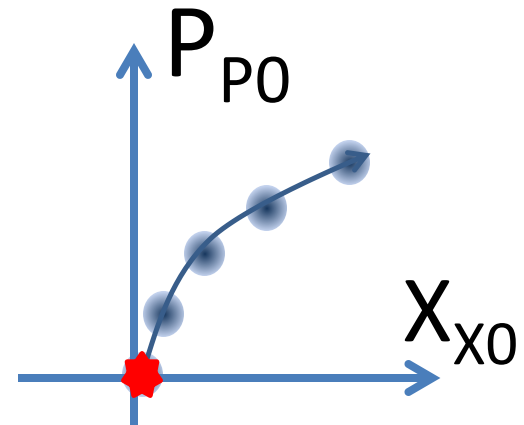
$P+P_0, X-X_0$ – commuting variables
can be measured precisely



Beyond SQL

$$\begin{aligned} X(t)_{X_0} &= X(0)_{X_0} + (\dot{X} - \dot{X}_0)t \\ &= X(0)_{X_0} + (P + P_0)t/m = \\ &= X(0)_{X_0} + \text{classical dynamics} \end{aligned}$$

$$m_0 = -m$$

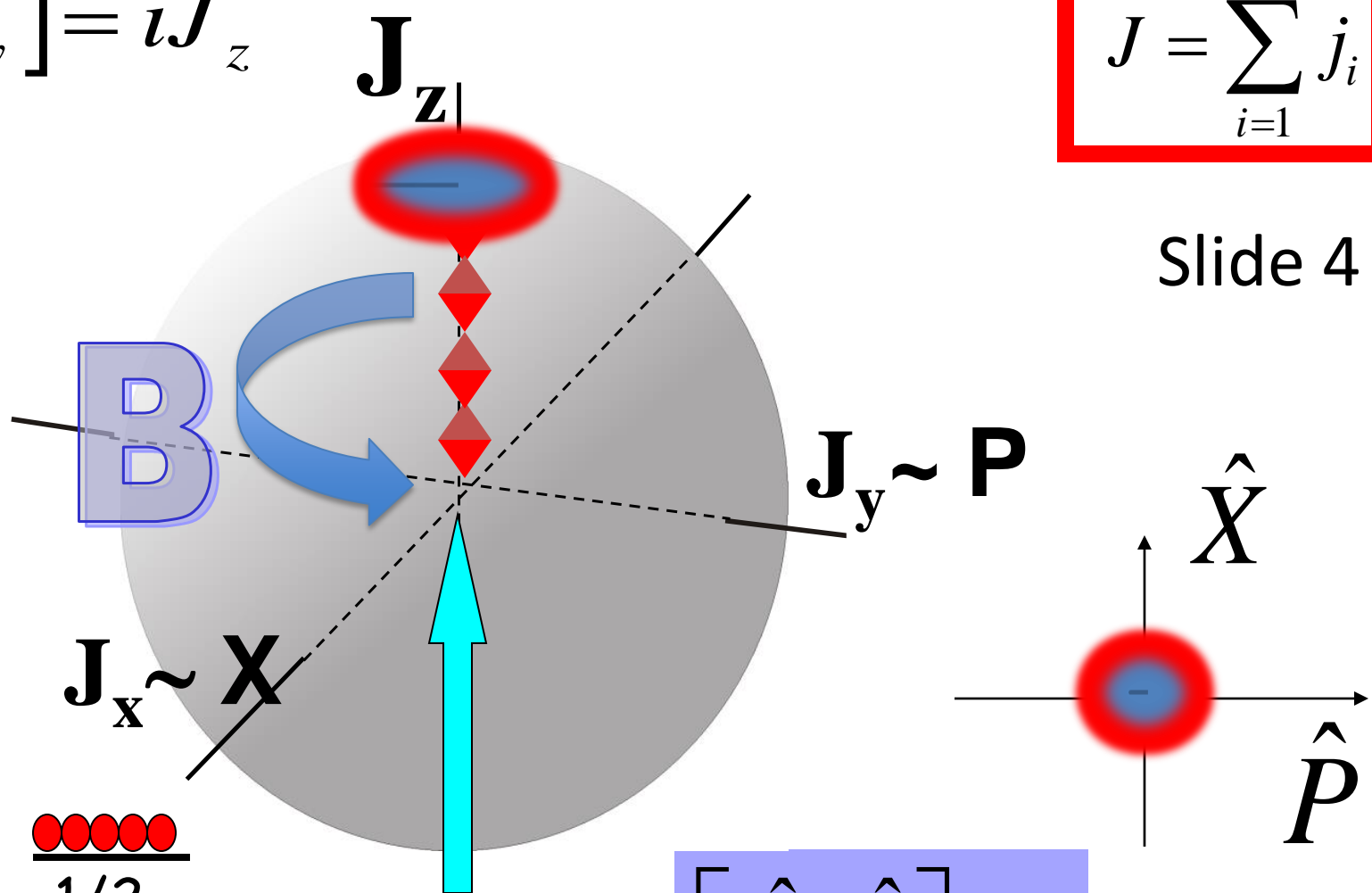


Spin ensemble = negative mass harmonic oscillator

$$[\hat{J}_x, \hat{J}_y] = iJ_z$$

$$J = \sum_{i=1}^N j_i$$

Slide 4



$-1/2$

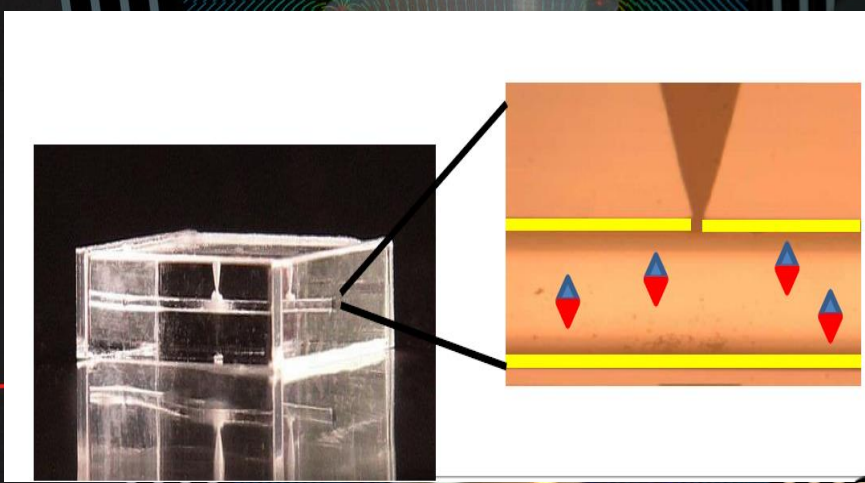
$1/2$

$$[\hat{X}, \hat{P}] = i$$

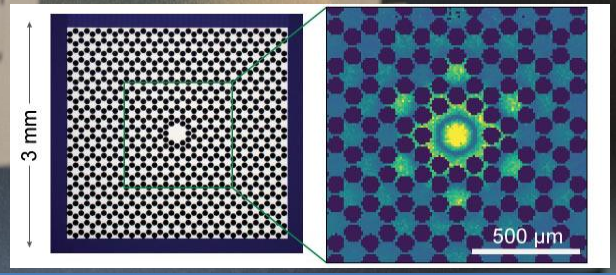
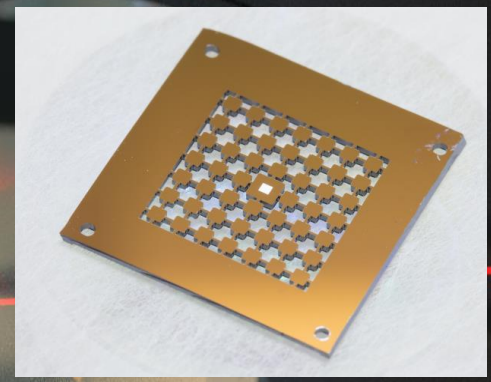
Negative mass oscillator

Holstein-Primakoff

Experimental demonstration for SPIN and Nano-MECHANICS



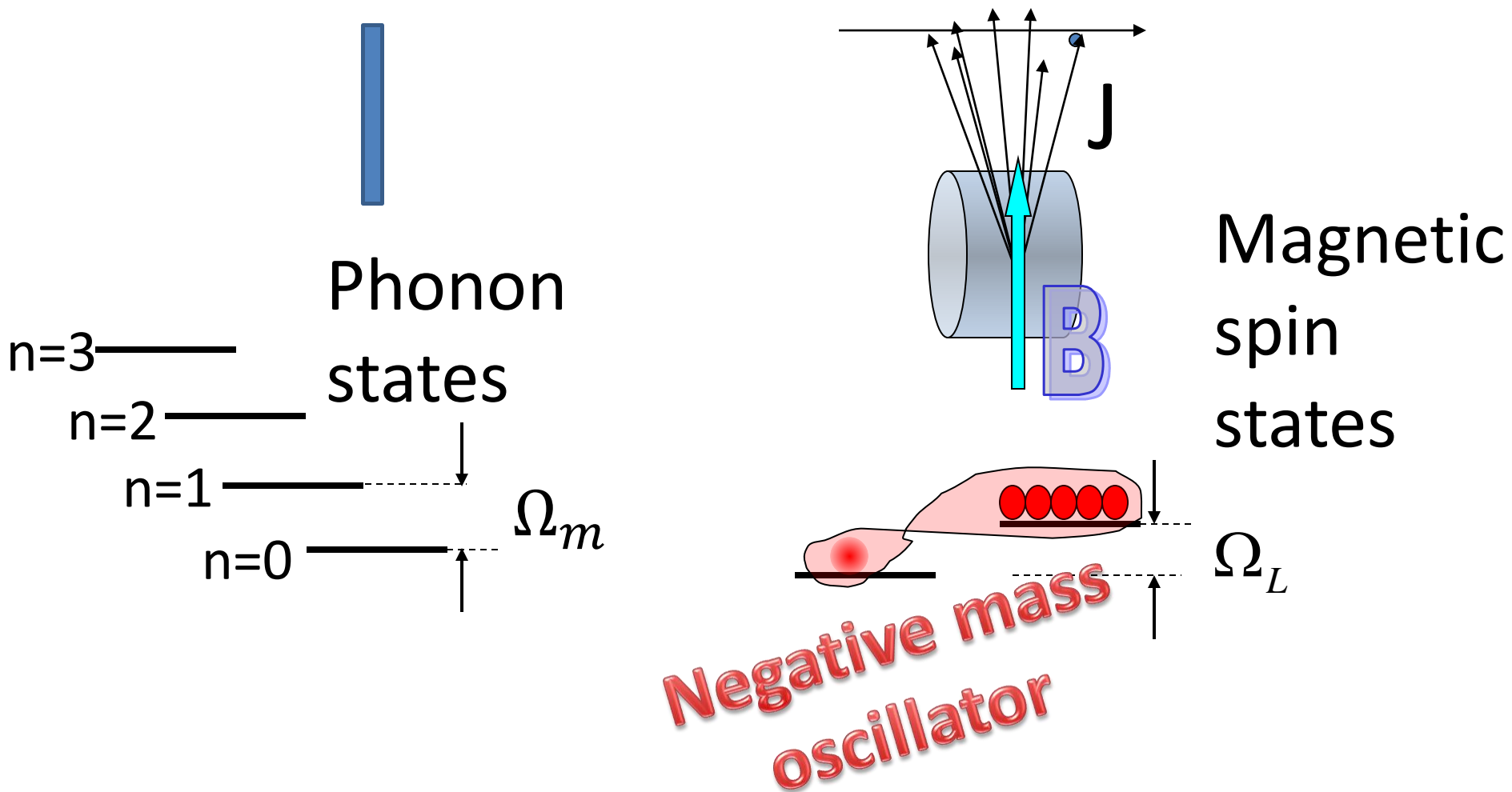
Room temperature spin quantum oscillator



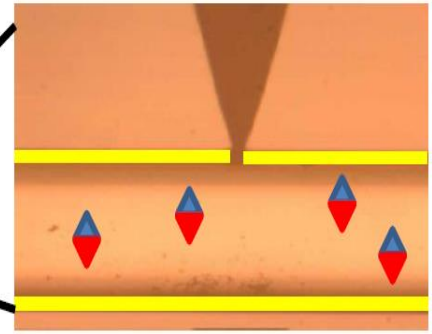
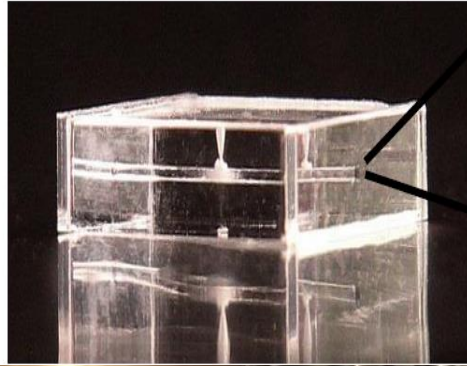
Mechanical oscillator with $Q = 1$ billion

Quantum back-action-evading measurement of motion in a negative mass reference frame

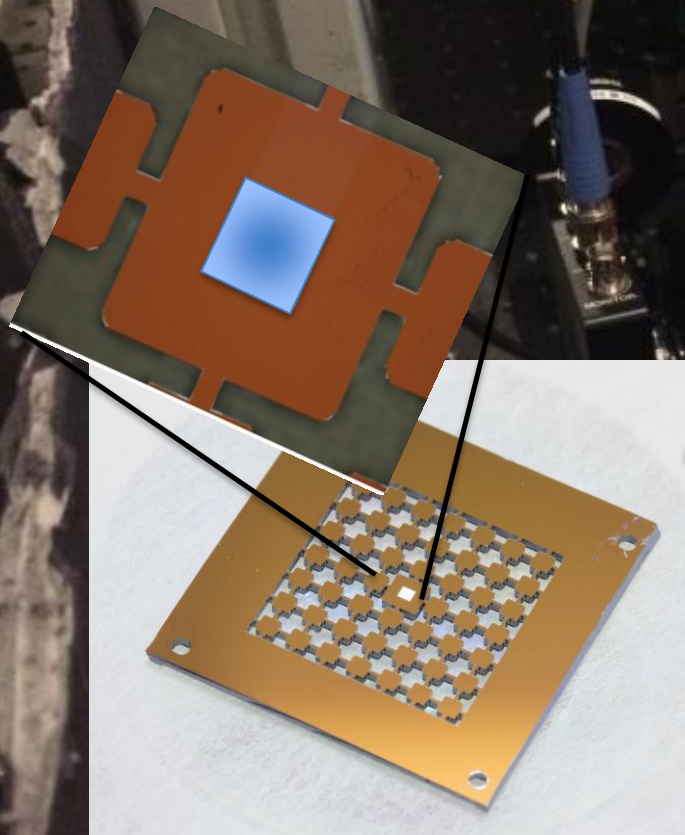
Christoffer B. Møller^{1*}, Rodrigo A. Thomas^{1*}, Georgios Vasilakis^{1,2}, Emil Zeuthen^{1,3}, Yeghishe Tsaturyan¹, Mikhail Balabas^{1,4}, Kasper Jensen¹, Albert Schliesser¹, Klemens Hammerer³ & Eugene S. Polzik¹



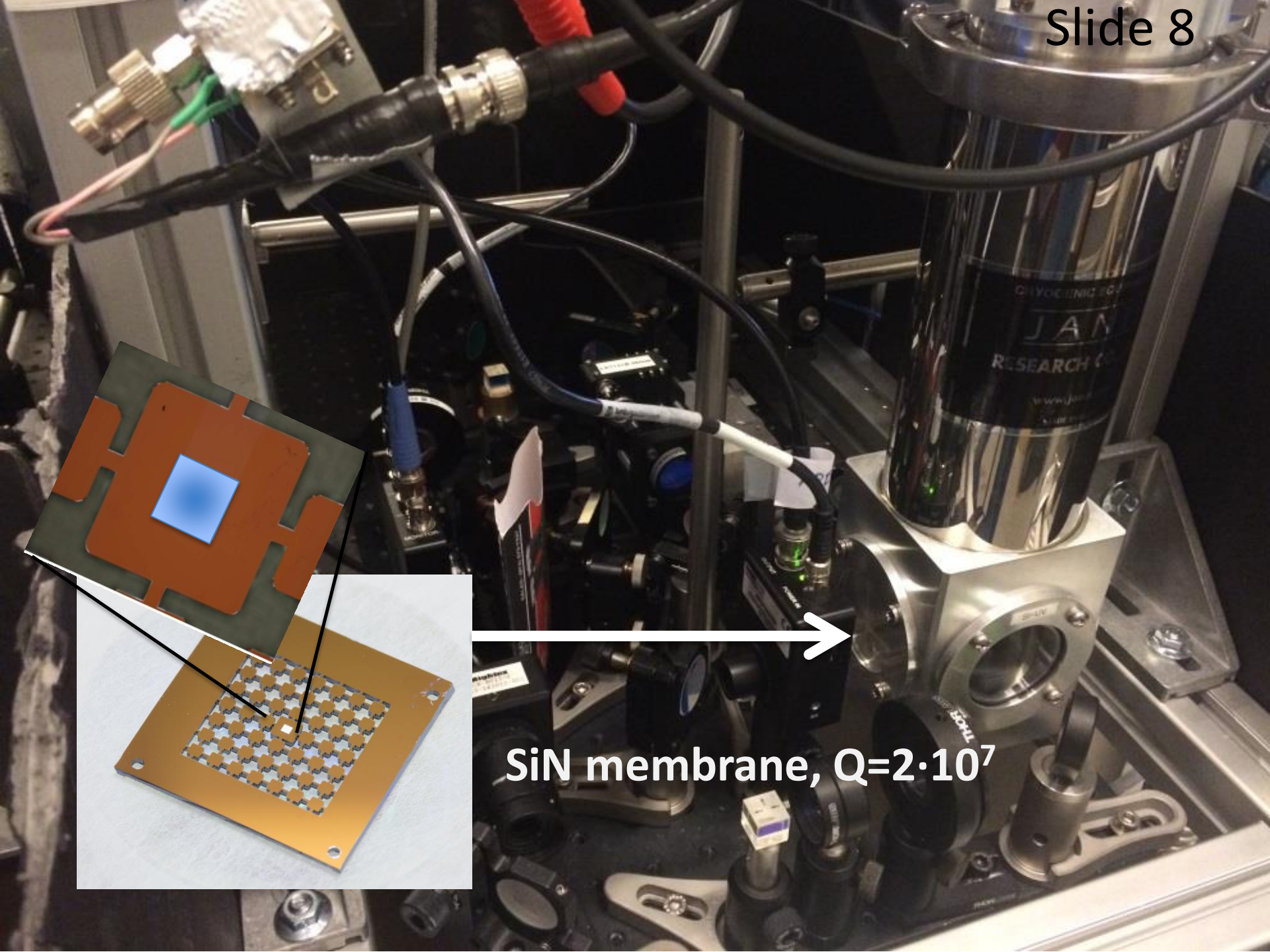
Slide 7



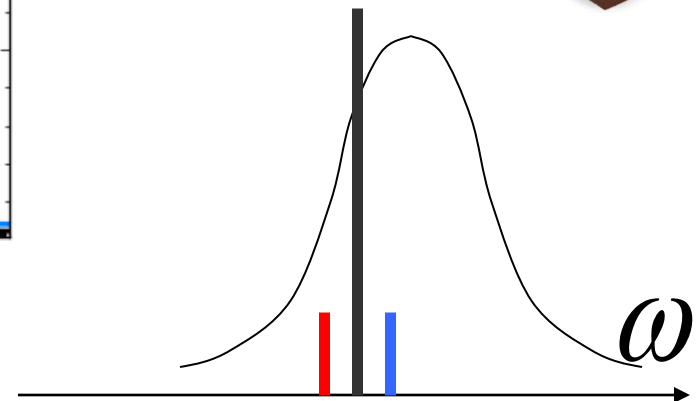
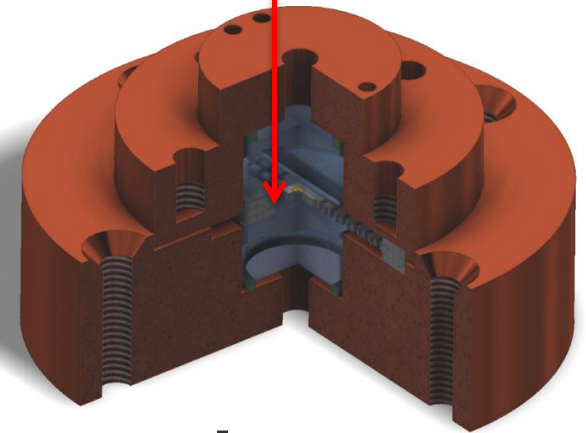
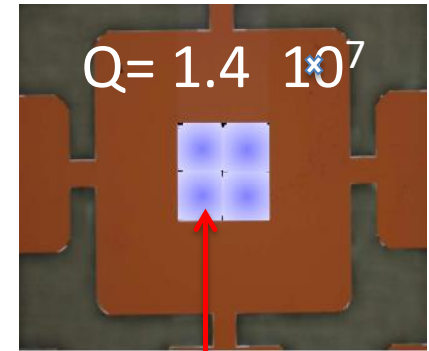
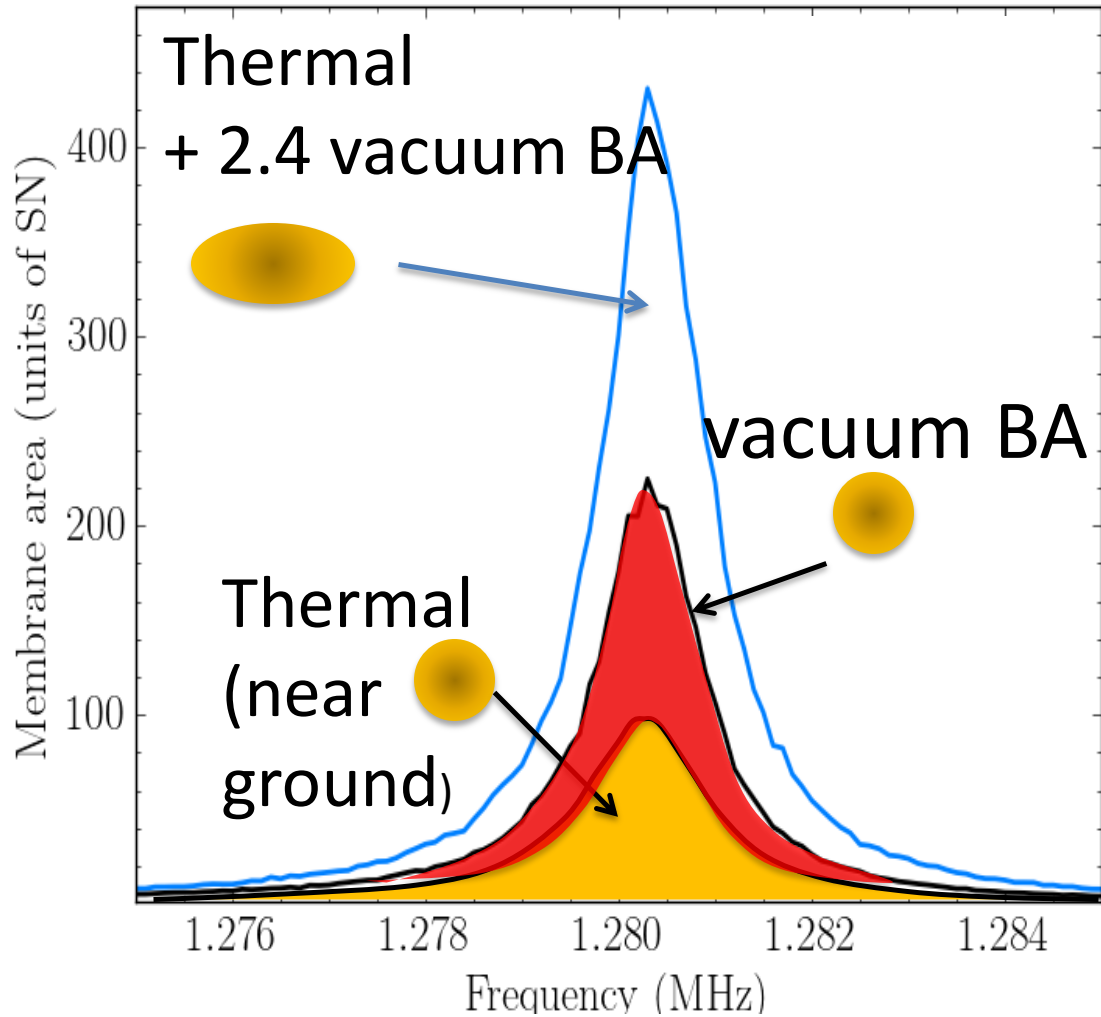
$$H = \Omega_L (P^2 + X^2) \Leftrightarrow -\Omega_L (J_z^2 + J_y^2) / J$$



SiN membrane, $Q=2 \cdot 10^7$



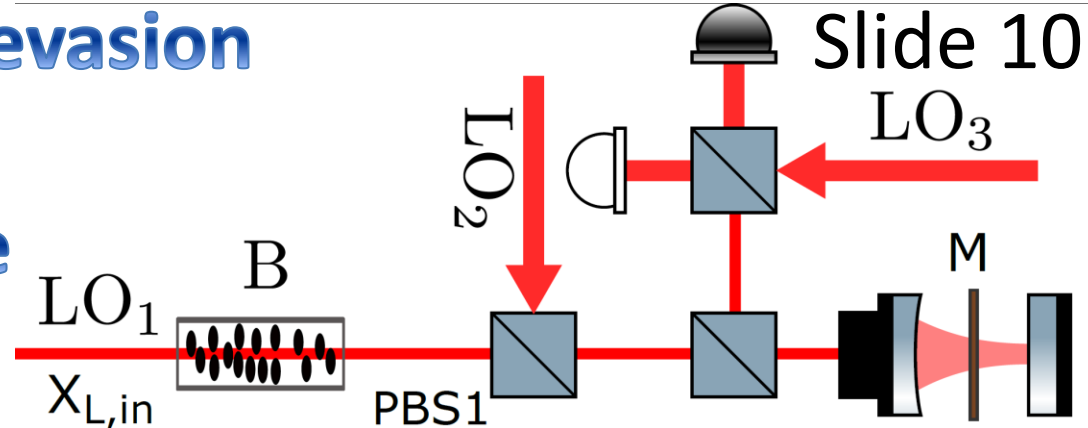
Mechanical oscillator. Cooling + Q back action



See also: Regal group, Science 2013; Stamper-Kurn group, Nat. Phys. 2016

Quantum back action evasion

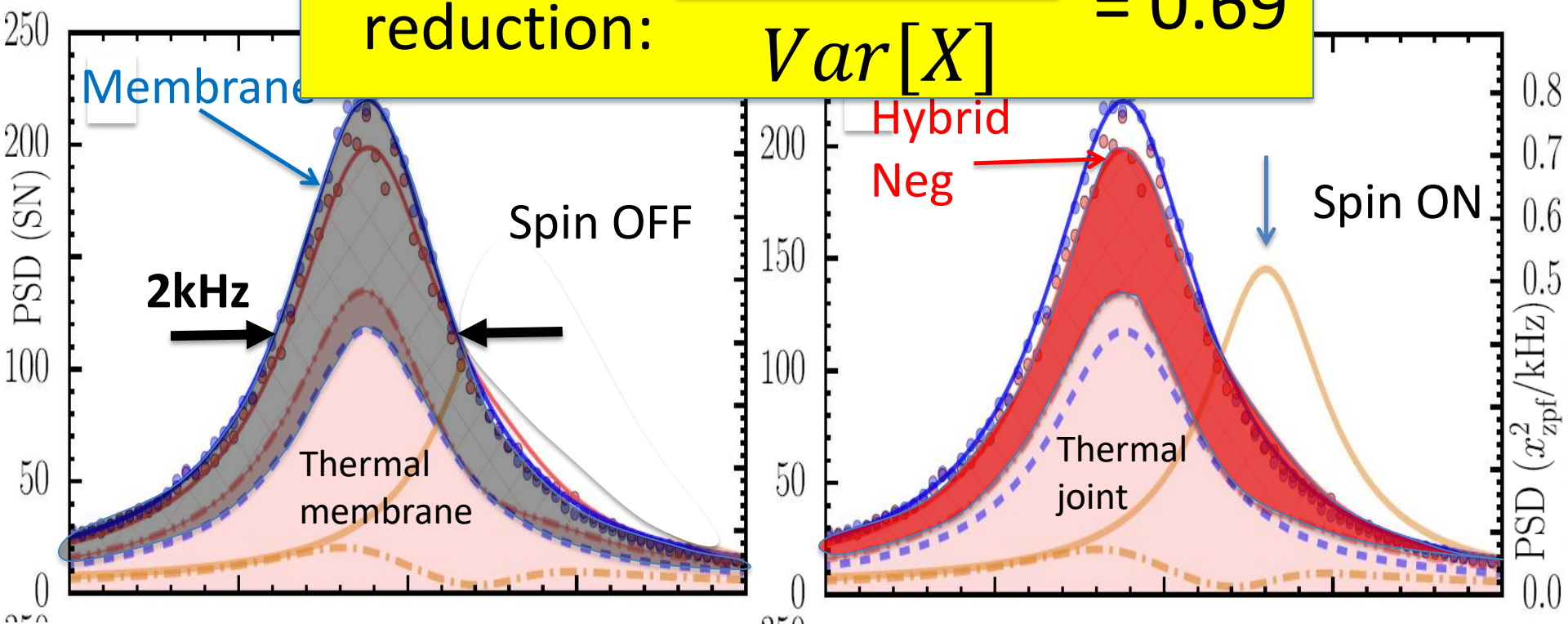
in the spin
reference frame



QBA

reduction:

$$\frac{\text{Var}[X - X_0]}{\text{Var}[X]} = 0.69$$

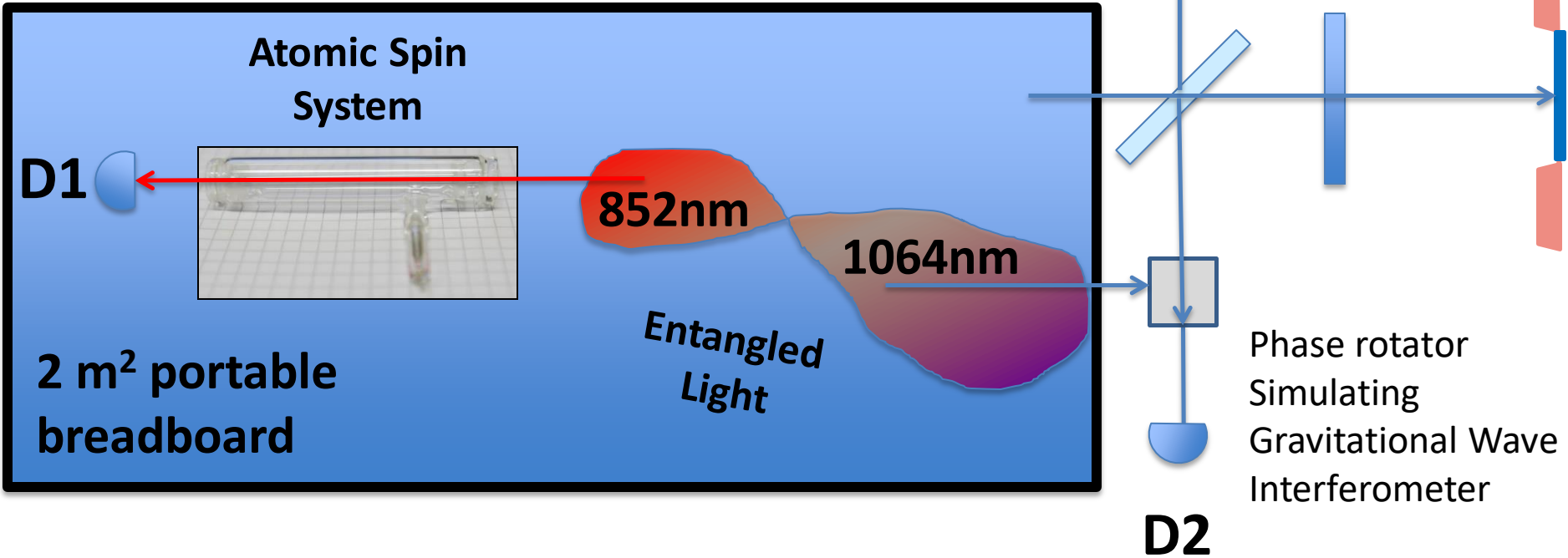


Proposal: F. Khalili and E.S.P. *Quantum back action evading detection of gravitational waves in a negative mass reference frame.* Phys. Rev. Lett. July 2018

Advanced proposal in preparation.

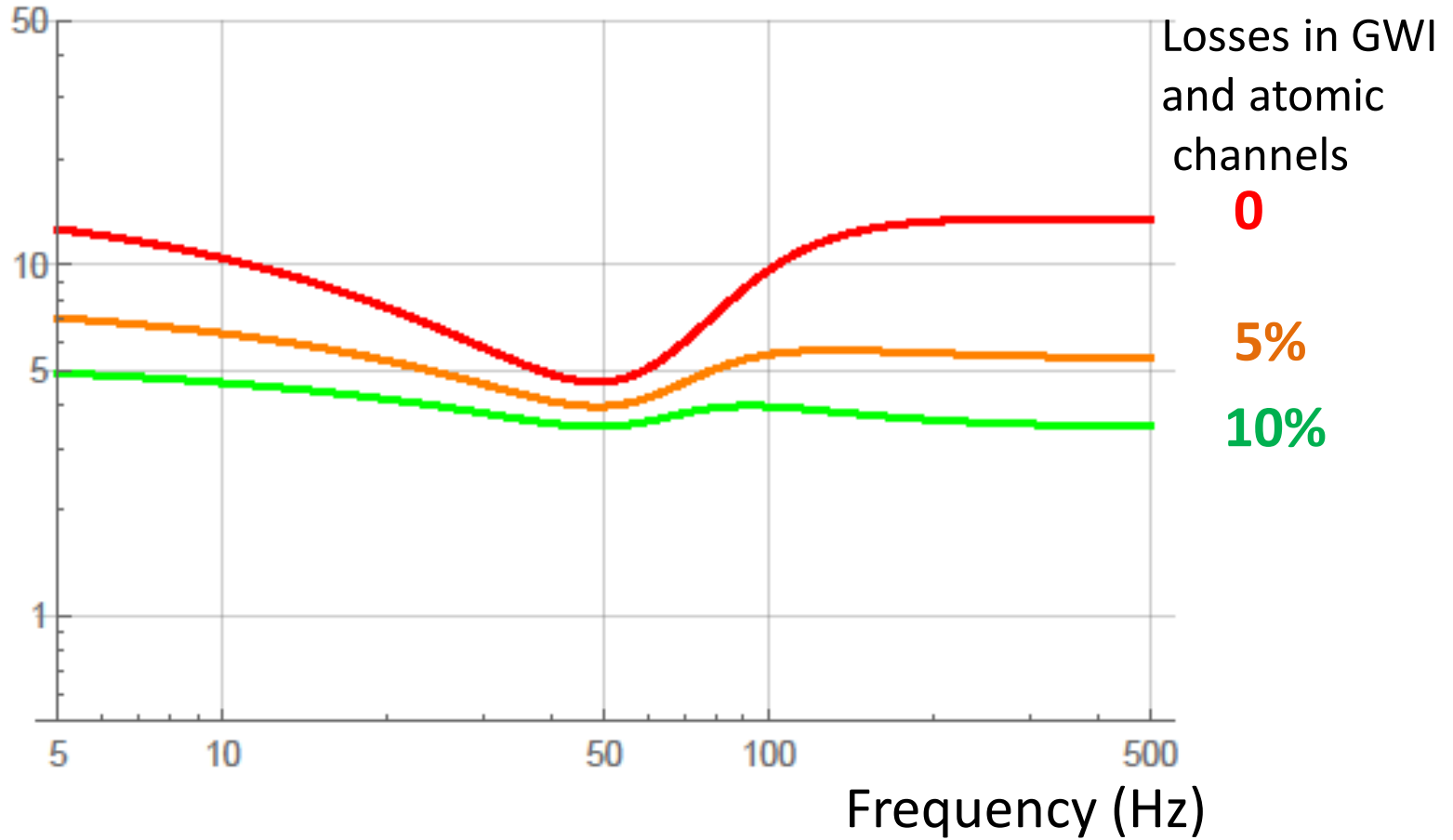
Gravitational Wave Interferometer

Slide 11

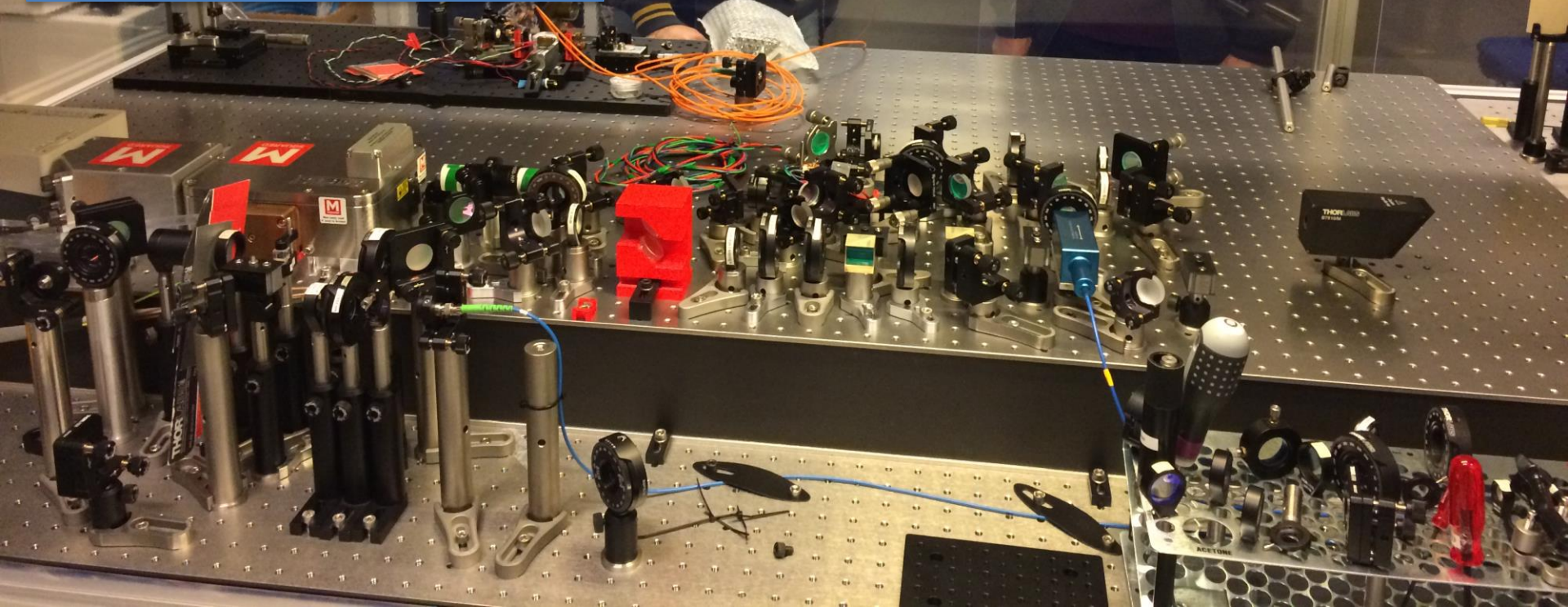
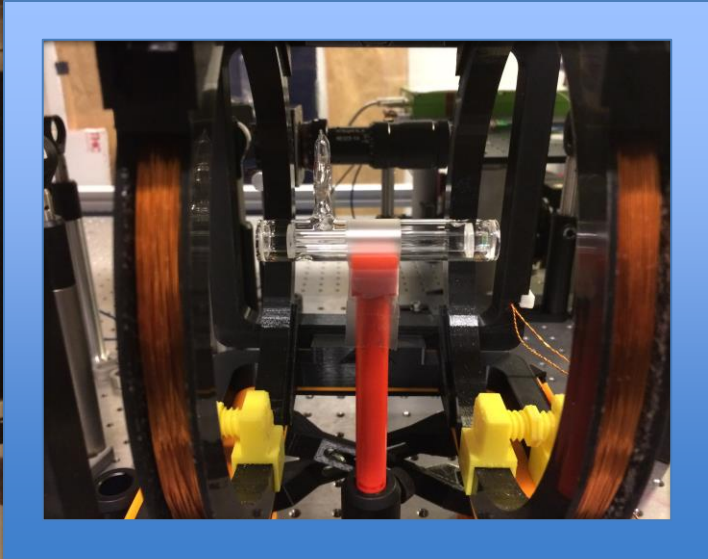


No change is GWD core optics required

Expected improvement in sensitivity (variance) for aLIGO
(ET – similar)



ET parameters taken from ET-0106C-10.pdf



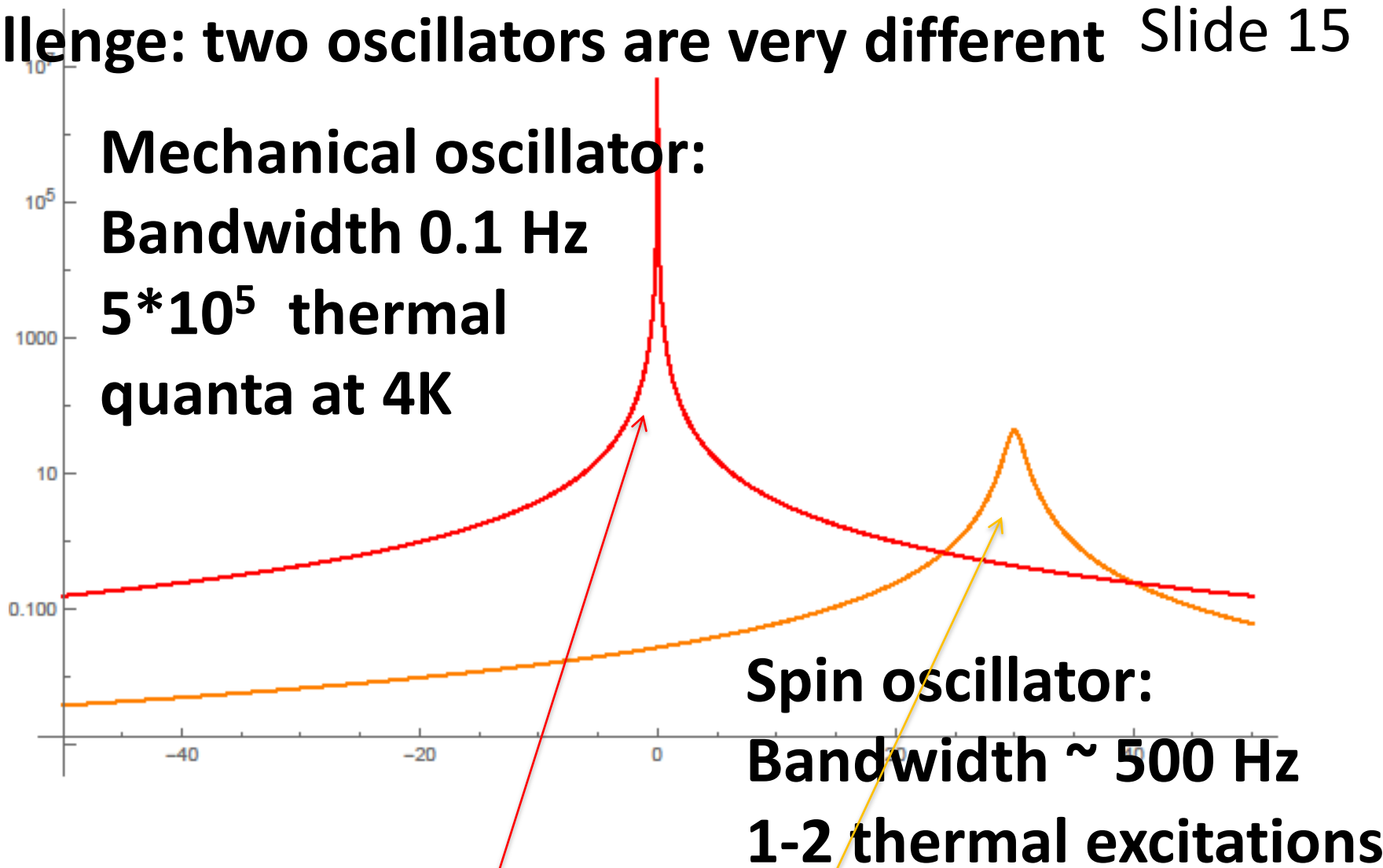
Summary:

Back action evasion for measurement of motion experimentally demonstrated

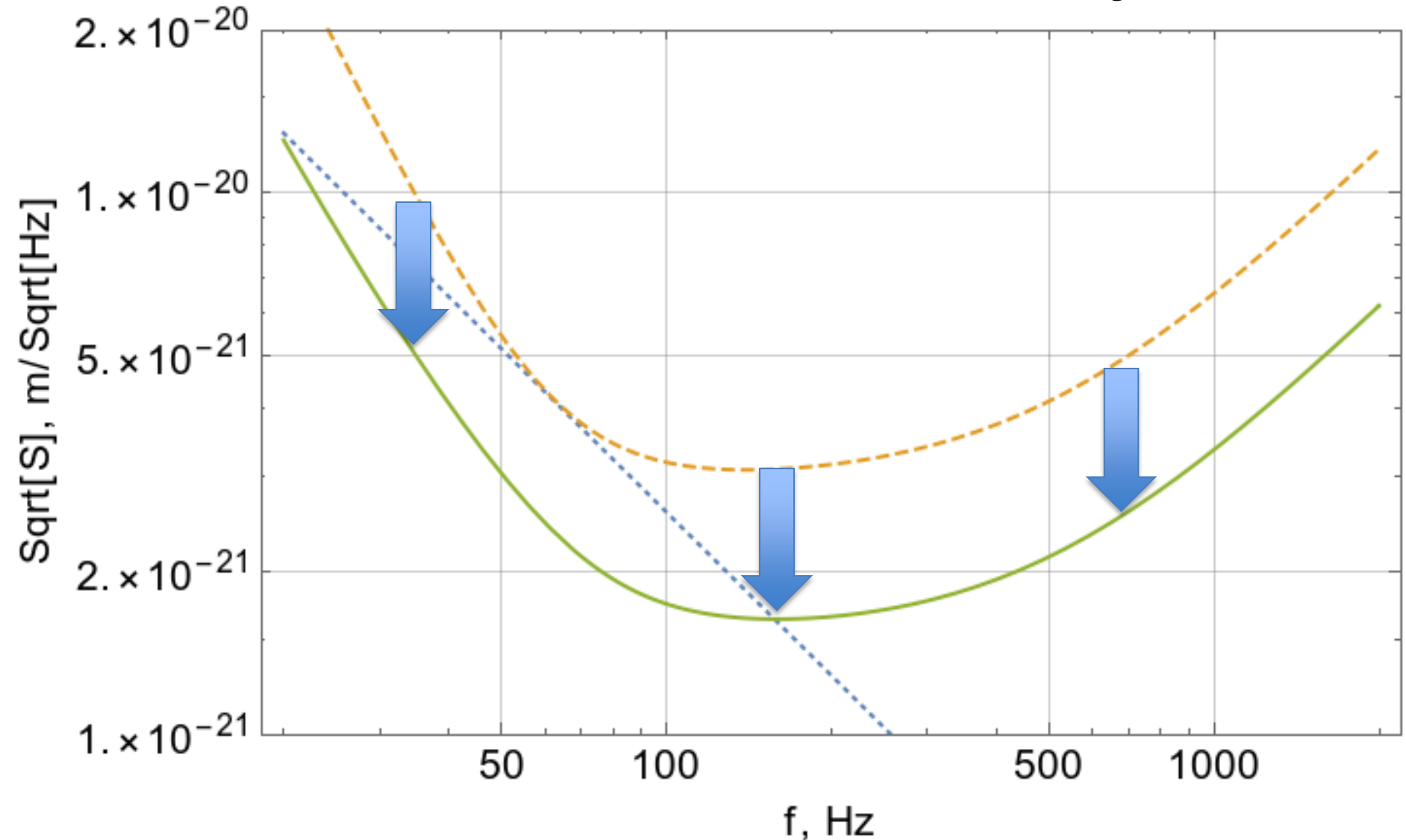
Status: entangled light source + atomic spin system for low frequency QBA evasion under construction

Challenge: as usual - optical losses

Challenge: two oscillators are very different Slide 15



$$\hat{P}_{L,\text{out}} = -\hat{P}_{L,\text{in}} - \sqrt{\Gamma_M \gamma_M \chi_M} \hat{F}_M + \sqrt{\Gamma_S \gamma_S \chi_S} \hat{F}_S + [\Gamma_M \chi_M + \Gamma_S \chi_S] \hat{X}_{L,\text{in}}^S$$

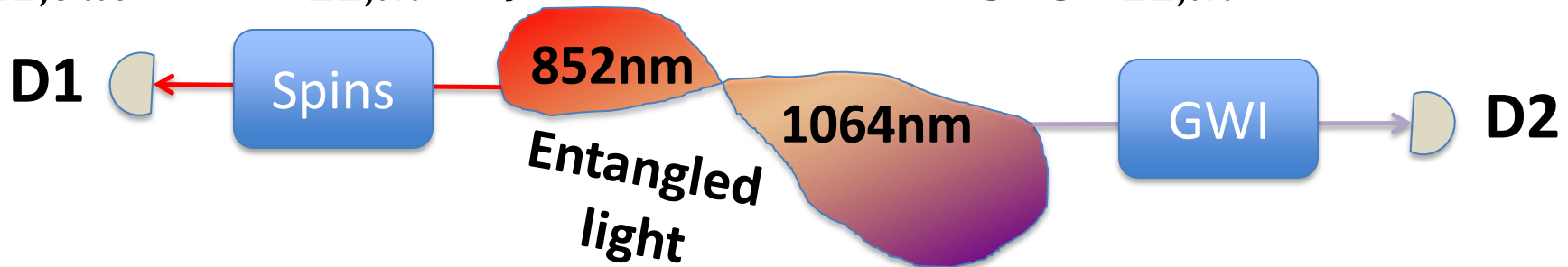
Simulation for LIGO

Probing the hybrid system with EPR entangled light modes

Slide 17

$$P_{L1,out} = -P_{L1,in} + \text{force terms} + \Gamma_M \chi_M X_{L1,in}$$

$$P_{L2,out} = -P_{L2,in} + \text{force terms} + \Gamma_S \chi_S X_{L2,in}$$



$$P_{L1,out} - P_{L2,out} = -P_{L1,in} + P_{L2,in} + \text{force terms} + \Gamma_M \chi_M X_{L1,in} - \Gamma_S \chi_S X_{L2,in}$$

$$\Gamma_S \chi_S = -\Gamma_M \chi_M \quad \Downarrow \quad \begin{aligned} (P_{L1,in} - P_{L2,in})^2 &= e^{-2r} \\ (X_{L1,in} + X_{L2,in})^2 &= e^{-2r} \end{aligned}$$

$$P_{L1,out} - P_{L2,out} \Rightarrow \text{force terms}$$

Measurement beyond SQL

1. Define trajectory relative to a quantum reference
2. Reference system has an effective negative mass
3. Entangled state of the reference and the probed systems is generated

See also:

Tsai and Caves, PRL 2010

M. Ozawa

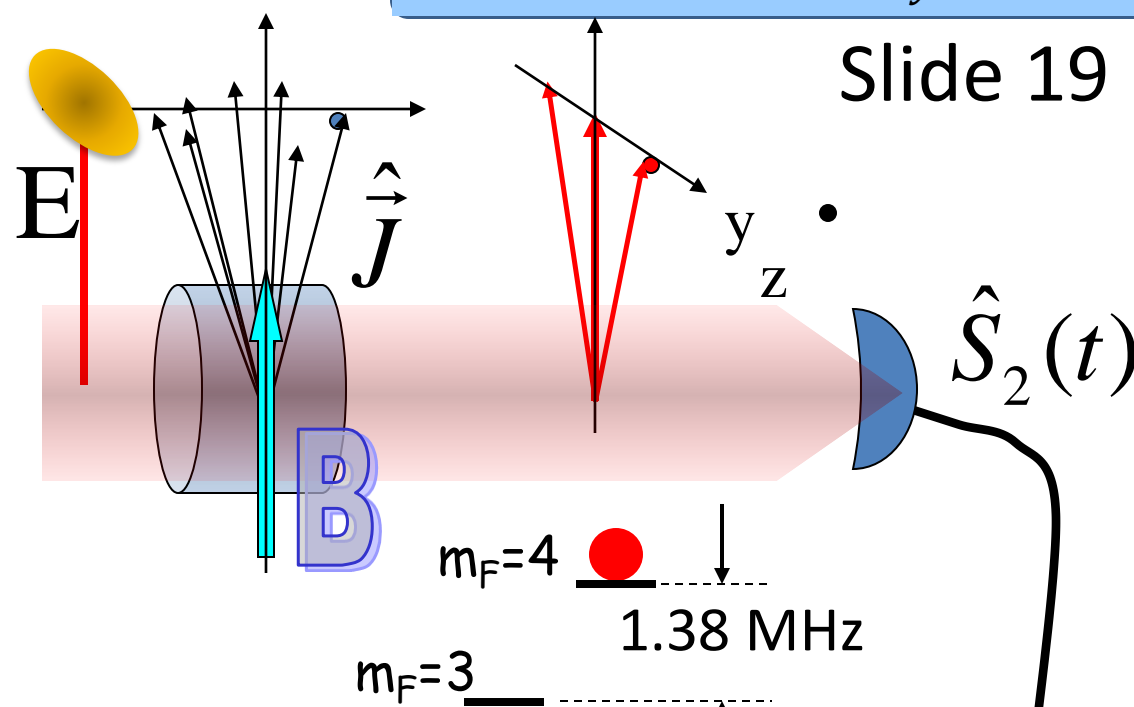
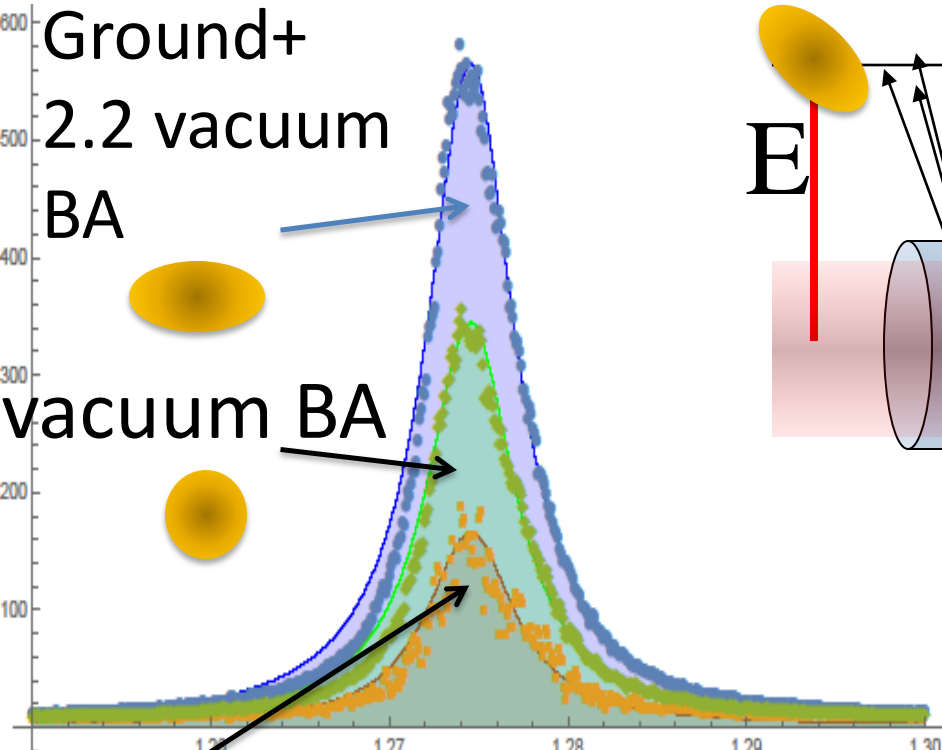
“Establishing Einstein-Podolsky-Rosen channels between nanomechanics and atomic ensembles”. K. Hammerer, M. Aspelmeyer, ESP, P. Zoller. **PRL** 102, 020501 (2009).

“Trajectories without quantum uncertainties”. K. Hammerer and ESP, **Annalen der Physik** . (2015)

Quantum back action onto spin oscillator

$$J_z^{lab} = J_z^{rot} \cos \Omega t - J_y^{rot} \sin \Omega t$$

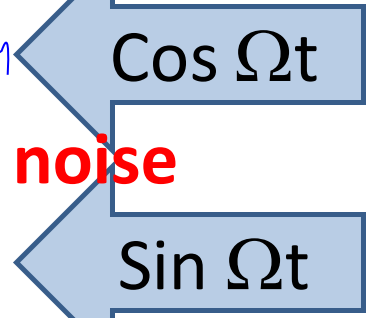
Slide 19



(Almost)
Ground
state

$$X \sim J_z^{rot}(t) + \text{Back action noise}$$

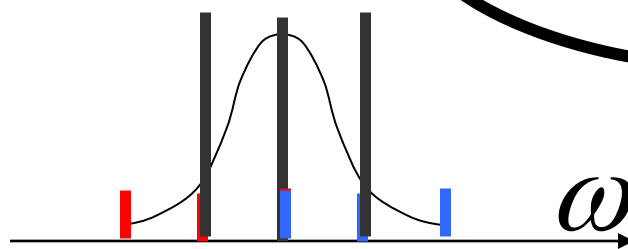
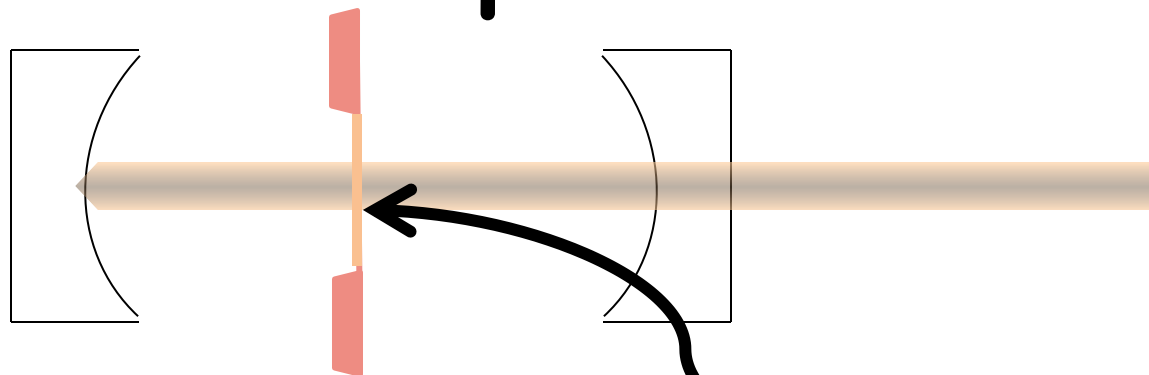
$$P \sim J_y^{rot}(t) + \text{Back action noise}$$



Lock-in
amplifier

Quantum Optomechanics

Slide 20



SiN membrane
high - Q

$$H = \chi_{Par} \hat{a}^\dagger \hat{b}^\dagger + \chi_{BS} \hat{a}^\dagger \hat{b} + h.c.$$
$$= g X_M X_L$$

phoTon

$$g = \chi_{Par} = \chi_{BS}$$

phoNon